Relic Antineutrino Capture

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Relic neutrinos

- As well as the 2.7 K microwave background radiation, the universe is filled with a sea of relic v's that decoupled from the rest of the universe within the first few seconds after the Big Bang.
- These relic v's may have played a crucial role in nucleosynthesis, structure formation and the evolution of the universe as a whole.

 \rightarrow A non-zero v mass can dramatically change the properties of the relic v sea and its role in the evolution of the universe.

 \rightarrow The current cosmological upper limit on the average v mass is ~0.2 eV (from Planck 2013). 2

Most copious relic particles

Relic photons(~3x10⁸⁷)

- They are bosons.
- They were decoupled when
 - the Universe was 4x10⁵ y old
 - the average energy was 0.25eV
 - the temperature was 3000 $^{\circ}\text{K}$
- As the Universe expanded their temperature dropped to 2.72 °K.
- It is higher because of reheating $e^+ + e^- \rightleftharpoons \gamma + \gamma$
- Today average energy
 → 6.3x10⁻⁴ eV

Relic neutrinos (~10⁸⁷)

- They are fermions.
- They were decoupled when
- the Universe was 1s old
- the average energy was 1MeV
- the temperature was $10^{10}\,^{\circ}\text{K}$
- As the Universe expanded their temperature dropped to 1.95 °K
- No reheating after 1s.
- Today average energy
 → 5.0x10⁻⁴ eV
- Nobody has yet seen relic neutrinos.

Relic neutrinos

- The low energy nuclear β or EC decays are excellent tools for testing non-zero v masses.
- Among all β unstable nuclides, ³H(Q_β=18.5906 32 keV), ¹⁸⁷Re(Q_β=2.4670 20 keV) & ¹⁶³Ho(Q_{EC}=2833(30stat)(15sys) eV) are attractive for 'non-zero v mass' experiment due to their low Q-values.
- Recently the interest in 163 Ho has been renewed because of a possible relic \overline{v} capture experiment.

Relic neutrino experiments

- Lusignoli & Vignati [']Relic v capture on ¹⁶³Ho decaying nuclei' [PLB 697, 11 (2011) & PLB 701, 673 (2011) (E)]
- Li & Xing, 'A possible detection of the cosmic v background in the presence of flavor effects' [PLB 698, 430 (2011)]
- Galeazzi et al., 'The electron capture decay of ¹⁶³Ho to measure the electron neutrino mass with sub-eV accuracy' [arXiv:1202.4763v3]
- Blaum et al., 'The electron capture ¹⁶³Ho experiment ECHo' [arXiv:1306.2655v1]
- S. Eliseev et al., 'Direct measurement of the mass difference of ¹⁶³Ho and ¹⁶³Dy solves the Q-value puzzle for the neutrino mass determination', PRL 115, 062501 (2015).

Relic neutrino experiments

• Vergados et al.,

'Prospects of detection of relic antineutrinos by resonant absorption in electron capturing nuclei.'
[J. Phys. G. Phys. 41 (2014)]
"¹⁵⁷Tb is a better candidate than ¹⁶³Ho." (?)

Experimental challenging techniques

- High Precision Penning Trap Mass Spectroscopy (PT-MS) [Blaum et al., Contemp. Phys. 51, 149 (2010)]
 S. Eliseev et al., 'Direct Measurement of the Mass Difference of ¹⁶³Ho and ¹⁶³Dy Solves the Q-Value Puzzle for the Neutrino Mass Determination', PRL 115, 062501 (2015)
 - This accurately measures the mass difference between the parent and the daughter nuclei.
- Microcalorimetry

[Gastaldo et al., Nucl. Instr. Meth. A 711, 150 (2013)]

- This measures the de-excitation spectrum.
- It analyzes the bolometric spectrum (γ and X-rays).
- The expected peaks will be well separated by a precision of a few eV.
- One hope to observe any relic antineutrino events at the tail. ⁷

Purpose

- Any other possible candidates for relic \overline{v} capture experiment?
- Relic \overline{v} capture by EC decaying nuclei.
 - EC decay
 - Relic \overline{v} capture
- Apply to ¹⁶³Ho, ²⁴³Cm, ¹⁵⁷Tb.
- Show all possible candidates for relic \overline{v} capture experiment.

Electron Capture (EC) decay

EC : inverse beta decay



E_i : de-excitation energy of *i*-th atomic shell (K,L,M,..), corresponding to the electron hole B.E. of the daughter atom → measurable!

Reaction rate for EC decay

$$(A,Z) \rightarrow (A,Z-1)^* + v_e \rightarrow (A,Z-1) + E_i + v_e$$

$$\lambda_{EC} = \frac{G_{\beta}^2}{4\pi^2} \sum_{i} n_i C_i \beta_i^2 B_i (Q - E_i) \sqrt{(Q - E_i)^2 - m_v^2}$$

 $G_{\beta} = G_F \cos \theta_C$

- n_i : fraction of occupancy of the *i*-th atomic shell
- C_i : nuclear shape factor (~all equal in an allowed transition)
- β_i : Coulomb amplitude of electron radial wave function
- B_i : atomic correction for electron exchange and overlap (~1)

Discrete energy spectrum

• In principle, the energy spectrum is given by a series of lines.

- The δ ft. does not allow to measure the spectrum endpoint.
- EC is not sensitive to neutrino mass features at the endpoint.

Uncertainty relation

 Atomic levels have finite widths.
 → δ-function should be replaced by a Breit-Wigner. (De Rùjula, Lusignoli, 1982)

$$\frac{d\lambda_{EC}}{dE_{c}} = \frac{G_{\beta}^{2}}{4\pi^{2}} (Q - E_{c}) \sqrt{(Q - E_{c})^{2} - m_{v}^{2}}$$

$$\times \sum_{i} n_{i} C_{i} \beta_{i}^{2} B_{i} \frac{\Gamma_{i}}{2\pi} \frac{1}{(E_{c} - E_{i})^{2} + \Gamma_{i}^{2} / 4}$$

- This allows E to reach the Q-value and to produce a neutrino with zero energy.
- One needs a nucleus with an E_i close to Q-value to have small suppression from the Breit-Wigner.

Relic \overline{V}_{e} capture

Relic \overline{v}_{e} capture by EC decaying nucleus

- The crossed reaction with an incoming $\overline{V}_{\rm e}$ has no energy threshold.
- The nucleus can absorb the \overline{v}_{e} with zero energy.



 E_i : de-excitation energy of *i*-th atomic shell (K,L,M,..) \rightarrow measurable!

Reaction rate for \bar{v}_{e} capture

$$\overline{\mathbf{v}}_{e} + (A,Z) \rightarrow (A,Z-1)^{*} \rightarrow (A,Z-1) + \mathbf{E}_{i}$$

$$\lambda_{\overline{v}} = n_{\overline{v}} \frac{G_{\beta}^2}{2} \sum_{i} n_i C_i \beta_i^2 B_i \rho_i(E_{\overline{v}})$$

 $G_{\beta} = G_F \cos \theta_C$

- $n_{\overline{v}}(=n_v)$: # density of incoming \overline{v} 's (~55/cm³)
- $E_{\overline{v}}$: energy of incoming relic \overline{v} 's ($\simeq m_v$ for CvB)
- β_i : Coulomb amplitude of electron radial wave function
- B_i : atomic correction for electron exchange and overlap(~1)
- $\rho_i(E_{\overline{v}})$: density of final state per energy (Breit-Wigner form)

Interaction rate of relic \overline{V}_{e} and EC

$$\frac{\lambda_{\overline{v}}}{\lambda_{EC}} \simeq 2\pi^2 n_{\overline{v}} \frac{\sum_i n_i \beta_i^2 B_i \rho_i(E_{\overline{v}})}{\sum_i n_i \beta_i^2 B_i (Q - E_i)^2}$$

 $n_{\overline{v}}(=n_v)$: # density of incoming \overline{v} 's (~55/cm³)

- n_i : fraction of occupancy of *i*-th atomic shell
- β_i : Coulomb amplitude of electron radial wave function
- B_i : atomic correction for electron exchange and overlap (~1)
- $\rho_i(E_{\overline{v}})$: density of final state per energy

• 163Ho

- T_{1/2}: 4570 ± 25 y
- Q_{EC}: 2.80 ± 0.05 keV (Gatti et al., 2008)
 2.555 ± 0.016 keV (Reich & Singh, 2011)
 2.833(30_{stat})(15_{svs}) keV (Eliseev et al., 2015)
- EC decay of ¹⁶³Ho

$${}^{163}_{67}\text{Ho} \rightarrow {}^{163}_{66}\text{Dy}_{i}^{*} + v_{e} \rightarrow {}^{163}_{66}\text{Dy} + E_{i} + v_{e}$$

• Relic \overline{v}_{e} capture on ¹⁶³Ho

$$\overline{v}_{e} + {}^{163}_{67}\text{Ho} \rightarrow {}^{163}_{66}\text{Dy}_{i}^{*} \rightarrow {}^{163}_{66}\text{Dy}_{i} + E_{i}$$

The Q -value for EC decay of ${}^{163}_{67}$ Ho is so small that only electrons from the following levels can be captured.

Energy levels & their widths of the captured electrons, for ¹⁶³₆₆Dy.

Level	E_i (eV)	Γ_i (eV)
M ₁ [3S]	2047	13.2
M ₂ [3P _{1/2}]	1842	6.0
N ₁ [4S]	414.2	5.4
N ₂ [4P _{1/2}]	333.5	5.3
O ₁ [5S]	49.9	3
O ₂ [5P _{1/2}]	26.3	3

Electrons squared wave functions at the origin β_i^2 relative to β_{3S}^2 [I.M. Band et al., At. Data. Nucl. Data Tables 35, 1 (1986).]

LevelsRatio3S / 3S1.0 $3P_{1/2} / 3S$ 0.05264S / 3S0.232 $4P_{1/2} / 3S$ 0.01195S / 3S0.0345 $5P_{1/2} / 3S$ 0.00156S / 3S0.0021

For given principle quantum number, electron squared wave function of S-state (l=0) is much larger than the one of P_{1/2} state.

Energy spectrum in EC decays of 163 Ho [Q=2.5 keV] \rightarrow De-excitation energy spectrum of 163 Dy*



19

Energy spectrum in EC decays of 163 Ho [Q=2.5 keV] \rightarrow De-excitation energy spectrum of 163 Dy*



De-excitation energy spectrum of ¹⁶³Dy*



Interaction rate for ¹⁶³Ho



Q_{EC}: 2.80 ± 0.05 keV (Gatti et al., 2008) 2.555 ± 0.016 keV (Reich & Singh, 2011)

2.833(30_{stat})(15_{sys}) keV (Eliseev et al., 2015)

Q-value	2.2 keV	2.5 keV	2.8 keV	2.833 keV
$\lambda_{\overline{v}}$ / $\lambda_{_{EC}}$	7.6×10 ⁻²²	5.8×10 ⁻²³	1.4×10 ⁻²³	1.2×10 ⁻²³

 \rightarrow Very sensitive to Q-value !

For Q=2.833 keV

For 10 events per year \rightarrow We need 1.46 ton ¹⁶³Ho source.

Feasibility

- If there is no overdensity $\left(=\frac{\rho(x)-\overline{\rho}}{\overline{\rho}}\right)$ in the v distribution, the detection is not possible.
- Kaboth et al., [PRD82, 2010]
 "If the overdensity is > 2x10⁹,
 KATRIN experiment may be able to detect relic neutrinos"
- The overdensity is expected to be less than ~10⁴, which is the matter overdensity in our galaxy.

[Ringwald & Wong, JCAP 0412, 005 (2004)]

- Krauss & Grashow [Nature 310, 19(1984)] & others
 - \rightarrow do not consider
 - decay to excited state (meta-stable state)
 - electron states with higher principal quantum numbers.
- Meta-stable state
 - T_{1/2} > 10⁻⁹ s
 - Occasionally, $T_{1/2}$ is far longer.

[lasting minutes, hours, or 10¹⁵ years for ^{180m}Ta.]

We checked whether there would be any other candidates for the relic \overline{v} capture experiment with calculations of Q-value for EC with allowed selection rule including

- all electron states including higher principal quantum numbers, K, L, M, N, O, P,
- excited states of daughter nuclei (meta-stable state)



Going to Ground State

$$Q_{\text{EC}} = \Delta m_{(Z)} - \Delta m_{(Z-1)}' \quad (': \text{ atomic excitation})$$
$$= \Delta m_{(Z)} - \left[\Delta m_{(Z-1)} + B_{(Z-1).e} - B_{(Z-1).e-last}\right]$$
$$= \Delta m_{(Z)} - \Delta m_{(Z-1)} - B_{(Z-1).e} + B_{(Z-1).e-last}$$
$$dQ_{\text{EC}} = \sqrt{\Delta m_{(Z)}^2 + \Delta m_{(Z-1)}^2}$$

- Considered EC from all electron levels, K, L,M,N,O,P, (I=0,1,2,3,4,...) - Q_{FC} < 60 keV

Other candidates (for going to ground states)

New AME data (Audi et al., 2013)

N Z A EL	MASS EXCI	ESS	B.E. /A	DE	ECAY	ENERGY
97 66 163 Dy	-66379.861	1.883	8161.777	0.012	β-	-2.555
96 67 163 Ho	-66377.306	1.883	8156.962	0.012	β-	-1210.729
93 64 157 Gd	-70822.822	1.623	8203.500	0.010	β-	-60.044
92 65 157 Tb	-70762.778	1.649	8198.134	0.011	β-	-1339.145
124 81 205 TI	-23820.349	1.329	7878.392	0.006	β-	-50.632
123 82 205 Pb	-23769.717	1.239	7874.328	0.006	β-	-2705.559
148 95 243 Am	57176.315	2,266	7530,168	0.009	ß-	-7,473
147 96 243 Cm	57183.788	2.052	7526.918	0.008	β-	-1507.591
116 77 193 lr	-34538 319	1 932	7938 144	0.010	ß-	-56 628
115 78 <mark>193 Pt</mark>	-34481.690	1.952	7933.797	0.010	β -	-1075.761

A new candidate – ²⁴³Cm

- ${}^{243}_{96}$ Cm ($\rightarrow {}^{243}_{95}$ Am)
 - T_{1/2}: 29.1 ± 0.1 y
 - Q_{EC}: 7.5 ± 1.7 keV (Akovali, NNDC, 2004)

7.473 ± 1.713 keV (Audi, 2013)

• EC decay of ²⁴³Cm

$${}^{243}_{96}\text{Cm} \rightarrow {}^{243}_{95}\text{Am}_{i}^{*} + v_{e} \rightarrow {}^{243}_{95}\text{Am} + E_{i} + v_{e}$$

• Relic \overline{V}_{e} capture on ²⁴³Cm

$$\overline{\mathbf{V}}_{e} + {}^{243}_{96}\text{Cm} \rightarrow {}^{243}_{95}\text{Am}_{i}^{*} \rightarrow {}^{243}_{95}\text{Am} + \mathbf{E}_{i}$$

Application to ²⁴³₉₆Cm

The Q -value for EC decay of ²⁴³₉₆Cm is so small that only electrons from levels M1, M2, N1, N2, O1, O2, P1, P2 can be captured.

Energy levels & their widths of the captured electrons, for ²⁴³₉₅Am.

Level	E_i (eV)	Γ_i (eV)
M ₁ [3S]	6133.0	16 [from ⁹² U]
M ₂ [3P _{1/2}]	5739.0	15 [from ⁹² U]
N ₁ [4S]	1620.3	13 [from ⁹² U]
N ₂ [4P _{1/2}]	1438.0	12 [from ⁹³ Np]
O ₁ [5S]	365.0	3
O ₂ [5P _{1/2}]	298.0	2
P ₁ [6S]	48.0	1
P ₂ [6P _{1/2}]	29.0	1

Application to ²⁴³₉₆Cm

Interaction rate for ²⁴³Cm



Q_{EC}: 7.5 ± 1.7 keV (Akovali, NNDC, 2004) 7.473 ± 1.713 keV (Audi, 2013)

Q-value	7.50 keV	7.47 keV	5.77 keV
$\lambda_{\overline{v}}$ / $\lambda_{_{EC}}$	6.88×10 ⁻²⁵	7.24×10 ⁻²⁵	3.44×10 ⁻²²

(Cf) 163 Ho : 1.2×10⁻²³, for Q_{FC}=2.833 keV

Are there other candidates for the relic \overline{v} capture experiment?

i) Consider EC from all electron states, K, L, M, N, O, P...

ii) Consider EC decay leading to excited states of daughter nuclei expecting resonant EC decay.

$$Q'_{EC} = \Delta m_{(Z)} - \Delta m_{(Z-1)}^{*'}$$

(': atomic excitation, *: nuclear excitation)
$$dQ'_{EC} = \sqrt{\Delta m_{(Z)}^{2} + \Delta m_{(Z-1)}^{2}}$$

$$\Delta Q'_{EC} = |Q'_{EC}| - dQ'_{EC}$$

<u>Conditions</u>: $T_{1/2} > 10$ days,

 Q'_{FC} <10 keV, dQ'_{FC} <10 keV, $\Delta Q'_{FC}$ <10 keV



New candidates (for going to excited states)?



New candidates (for going to excited states)?

Mother	$T_{1/2}$	$J_i \Pi_i$	Daughter	$J_f \Pi_f$	E_{excited}	Q'_{EC}	dQ'_{EC}	$\Delta Q'_{EC}$
					(keV)	(keV)	(keV)	(keV)
$^{103}\mathrm{Pd}$	16.991 d	5/2 +	103 Rh	5/2+	536.8	3.231	3.517	-0.287
$^{127}\mathrm{Xe}$	36.346 d	1/2 +	127I	3/2+	628.7	0.544	5.496	-4.952
$^{131}\mathrm{Ba}$	$11.50 {\rm d}$	1/2 +	^{131}Cs	3/2 *	1342.	-3.043	5.612	-2.569
$^{157}\mathrm{Tb}$	71 y	3/2 +	$^{157}\mathrm{Gd}$	5/2-	54.53	1.714	2.314	-0.600
$^{159}\mathrm{Dy}$	144.4 d	3/2-	$^{159}\mathrm{Tb}$	5/2-	363.5	-0.078	2.686	-2.608
$^{175}\mathrm{Hf}$	$70 \mathrm{d}$	5/2-	^{175}Lu	(7/2-)	672.9	-0.070	3.278	-3.208
$^{195}\mathrm{Au}$	180.098 d	3/2+	$^{195}\mathrm{Pt}$	1/2-	222.2	1.353	1.648	-0.295

(* 1/2+ , GEANT4 data)

 $\mathbf{Q'}_{\text{EC}} = \Delta m_{(Z)} - \Delta m_{(Z-1)}^{*} \quad (': \text{ atomic excitation, } *: \text{ nuclear excitation})$ $\mathbf{dQ'}_{\text{EC}} = \sqrt{\Delta m_{(Z)}^2 + \Delta m_{(Z-1)}^2}, \quad \Delta \mathbf{Q'}_{\text{EC}} = |\mathbf{Q'}_{\text{EC}}| - \mathbf{dQ'}_{\text{EC}}$

• Vergados et al.,

'Prospects of detection of relic antineutrinos by resonant absorption in electron capturing nuclei.'[J. Phys. G. Phys. 41 (2014)]

"¹⁵⁷Tb is a better candidate than ¹⁶³Ho." (?)

A new candidate - ¹⁵⁷₆₅Tb

- ${}^{157}_{65}$ Tb (\rightarrow ${}^{157}_{64}$ Gd)
 - T_{1/2}: 71 ± 7 y (NNDC, 2004)
 - Q_{EC}: 60.044 ± 0.297 keV (Audi, 2012)
 60.1 ± 0.3 keV (Helmer, NNDC, 2004)
- EC decay of ¹⁵⁷Tb

$${}^{157}_{65}\text{Tb} \rightarrow {}^{157}_{64}\text{Gd}_{i}^{*} + v_{e} \rightarrow {}^{157}_{64}\text{Gd} + E_{i} + v_{e}$$

• Relic \overline{V}_{e} capture on ¹⁵⁷Tb

$$\overline{V}_{e} + {}^{157}_{65}\text{Tb} \rightarrow {}^{157}_{64}\text{Gd}_{i}^{*} \rightarrow {}^{157}_{64}\text{Gd} + E_{i}$$

Application to ¹⁵⁷₆₅Tb

The Q -value for EC decay of ${}^{157}_{65}$ Tb is so small that only electrons from the following levels can be captured.

Energy levels & their widths of the captured electrons, for ¹⁵⁷₆₄Gd.

Level	E_i (eV)	Γ_i (eV)
K [1S]	50239.1	22.4
L ₁ [2P _{1/2}]	8375.6	3.8
L ₂ [2S]	7930.3	3.87
M ₁ [3S]	1880.0	12.8
M ₂ [3P _{1/2}]	1688.3	5.6
N ₁ [4S]	375.8	4.90
N ₂ [4P _{1/2}]	288.5	5.23
O ₁ [5S]	36.1	3
O ₂ [5P _{1/2}]	20.3	3

Application to ¹⁵⁷Tb

Interaction rate for ¹⁵⁷Tb (going to 54.5 keV excited state)

$$\frac{\lambda_{\overline{v}}}{\lambda_{EC}} \simeq 2\pi^2 n_{\overline{v}} \frac{\sum_{i} n_i \beta_i^2 B_i \rho_i(E_{\overline{v}})}{\sum_{i} n_i \beta_i^2 B_i (Q - E_i)^2}$$

Q_{EC}: 60.044 ± 0.297 keV (Audi, 2012) 60.1 ± 0.3 keV (Helmer, NNDC, 2004)

Q-value	5.511 keV	5.214 keV	5.808 keV
$\lambda_{\overline{v}}$ / $\lambda_{_{EC}}$	6.33×10-28	5.83×10-28	7.21×10-28

(Cf) 163 Ho : 1.2×10⁻²³, for Q_{EC}=2.833 keV

New possible candidates

For 10 events per year

Mother	$T_{1/2}$	Daughter	E_{excited}	$T_{1/2}$	$\lambda_{ar{ u}}/\lambda_{EC}$	Amount	Activity
	·		(keV)	(ps)		(kg)	(MCi)
$^{103}\mathrm{Pd}$	16.991 d	103 Rh	536.8	39	1.56×10^{-25}	7.4×10^{-1}	5.5×10^{1}
$^{127}\mathrm{Xe}$	$36.346 \ d$	$^{127}\mathrm{I}$	628.7	1.9	5.47×10^{-25}	7.9×10^{-5}	2.2×10^{-3}
^{131}Ba	11.50 d	^{131}Cs	1342.	-	2.96×10^{-26}	3.6×10^{-5}	3.1×10^{-3}
$^{157}\mathrm{Tb}$	71 y	$^{157}\mathrm{Gd}$	54.53	130	7.21×10^{-28}	370 t	1.2×10^{4}
$^{159}\mathrm{Dy}$	144.4 d	$^{159}\mathrm{Tb}$	363.5	153	2.62×10^{-21}	2.7×10^{-6}	1.6×10^{-5}
¹⁶³ Ho	$4570 { m y}$	$^{163}\mathrm{Dy}$	g.s.	Stable	1.22×10^{-23}	1.5×10^{3}	7.0×10^{-1}
$^{175}\mathrm{Hf}_1$	70 d	^{175}Lu	672.9	-	1.98×10^{-21}	2.0×10^{-5}	2.1×10^{-4}
$^{175}\mathrm{Hf}_2$	70 d	$^{175}\mathrm{Lu}$	684.3	-	2.25×10^{-17}	3.4×10^{-8}	3.6×10^{-7}
$^{195}\mathrm{Au}_1$	180.098 d	$^{195}\mathrm{Pt}$	211.4	49	9.96×10^{-25}	1.6×10^{-4}	5.8×10^{-4}
$^{195}\mathrm{Au}_2$	180.098 d	$^{195}\mathrm{Pt}$	222.2	-	1.99×10^{-24}	1.4×10^{-5}	5.1×10^{-5}
$^{243}\mathrm{Cm}$	29.1 y	^{243}Am	g.s.	7370 y	3.44×10^{-22}	4.9×10^{-1}	2.5×10^{-2}

All candidates

For 10 events per year



All candidates

For 10 events per year



Conclusions

- EC decaying nuclei can capture relic \overline{v} 's.
- However, the relic \overline{v} capture experiment is impossible for given overdensity in the $\overline{v}(v)$ distribution, which is expected to be less than ~10⁴ in our galaxy.
- We found other possible candidate nuclides with resonant EC decaying nuclides for CvB detection considering EC from all electron states including higher princi pal quantum numbers, K, L, M, N, O, P,
- EC going to ground state ; ¹⁶³₆₇Ho, (²⁴³₉₆Cm)
- EC leading to excited state of daughter nuclei ; ¹⁰³₄₆Pd,¹²⁷₅₄Xe, ¹³¹₅₆Ba,^{<u>157</u>₅₂Tb, ¹⁵⁹₆₆Dy,¹⁷⁵₇₂Hf, ¹⁹⁵₇₉Au.}

THANK YOU !!