

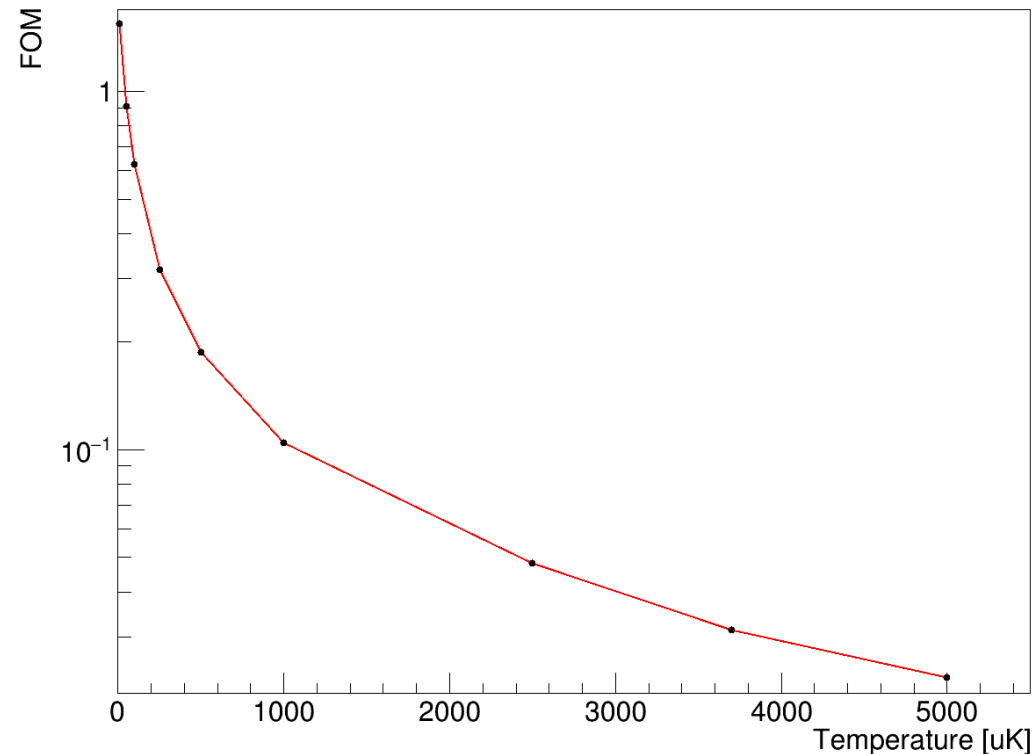
# Order of magnitude of energy

- Gravity (30cm fall) :  $\sim 10\text{neV}$
- $T = 10\mu\text{K}$  :  $\sim 1\text{neV}$
- $T = 0.5\text{mK}$  :  $\sim 10\text{neV}$
- $T = 5\text{mK}$  :  $\sim 100\text{neV}$
- No concern on EM scattering

# Figure of merit of upward-downward g

- $\frac{|T_{upward,mean} - T_{downward,mean}|}{(\sigma_{upward}^2 + \sigma_{downward}^2)^{0.5}} = \text{FOM}$

FOM with 50k ann.

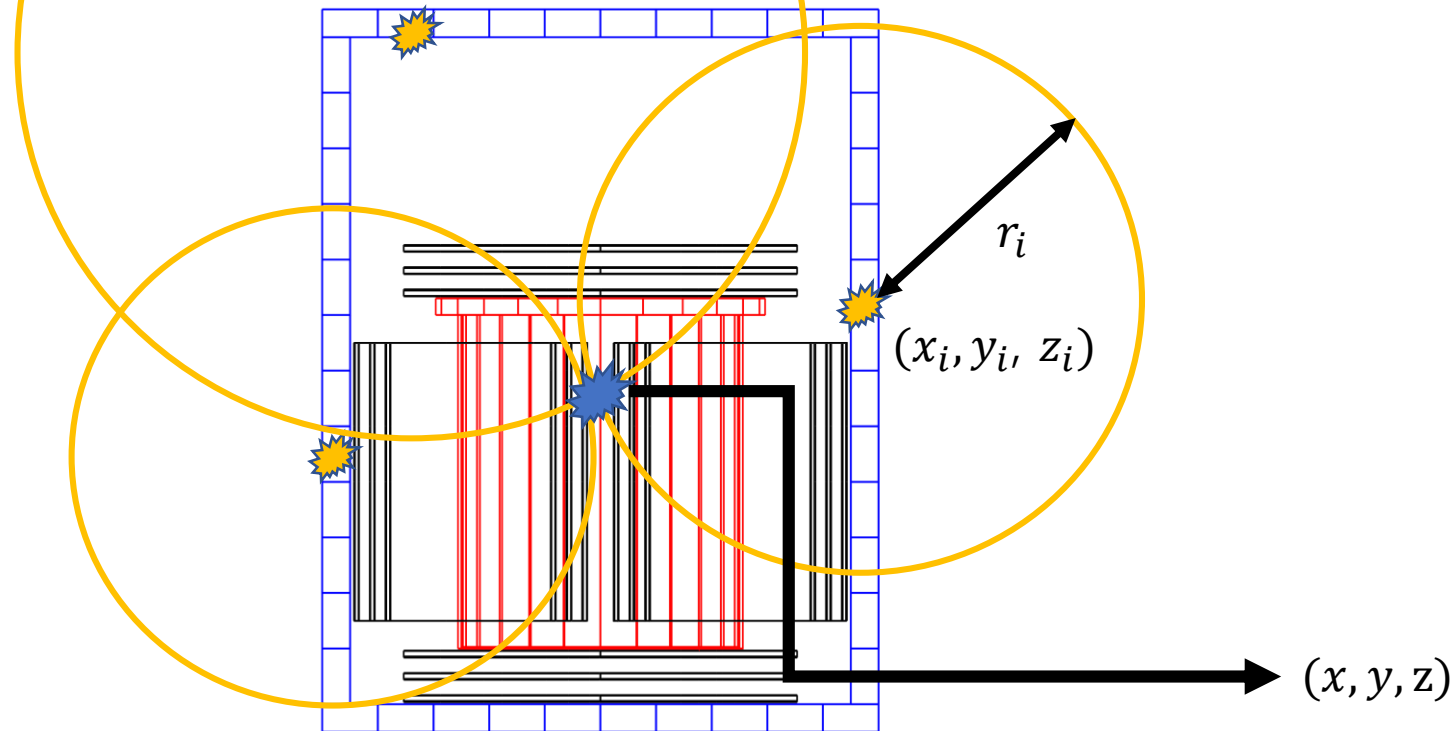


# Trilateration

- Find out the position of annihilation by using hit positions and flight lengths.
- 4 hits are needed to find the annihilation position.
- $<4$  hits give multiple solutions.
- But the trilateration needs the flight lengths of particles.
- Can we estimate flight lengths only using TOF data?

# Trilateration

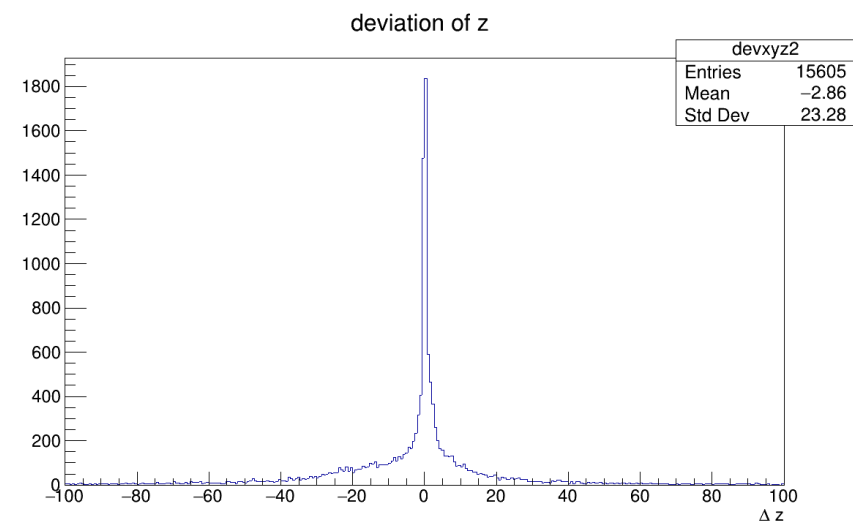
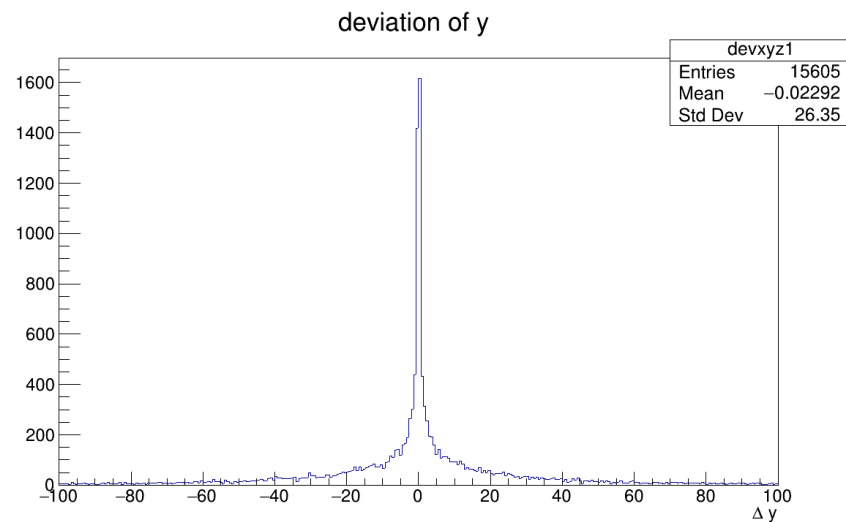
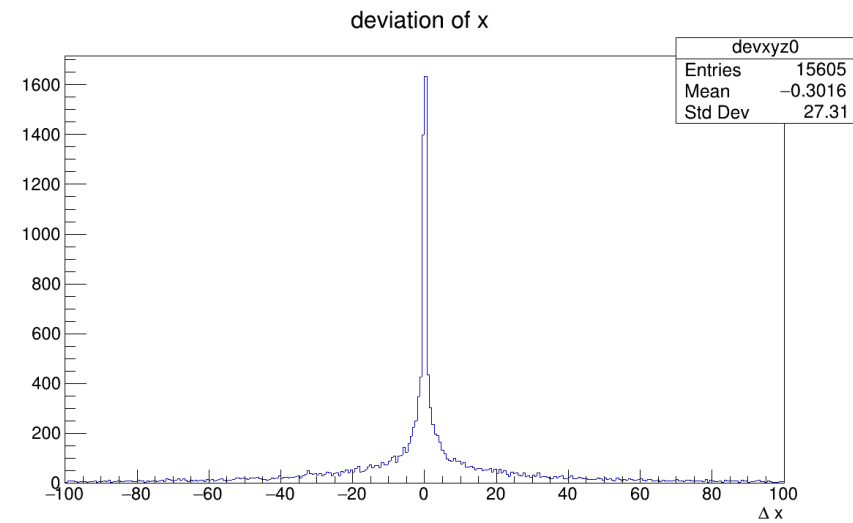
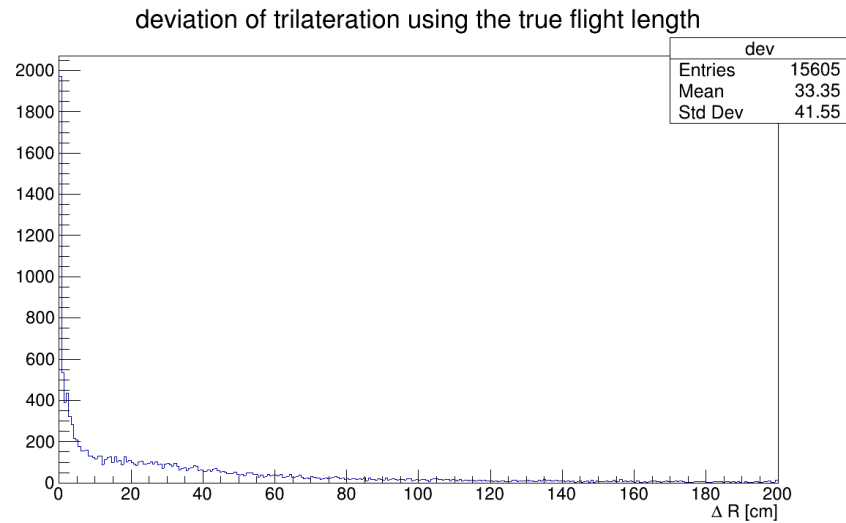
- $(x - x_i)^2 + (y - y_i)^2 + (z - z_i)^2 = r_i^2$  where  $i = 1, 2, 3, 4$
- $(-2x_i + 2x_{i+1})x + (-2y_i + 2y_{i+1})y + (-2z_i + 2z_{i+1})z = r_i^2 - r_{i+1}^2 - (x_i^2 + y_i^2 + z_i^2) + (x_{i+1}^2 + y_{i+1}^2 + z_{i+1}^2)$  where  $i = 1, 2, 3$



# Trilateration

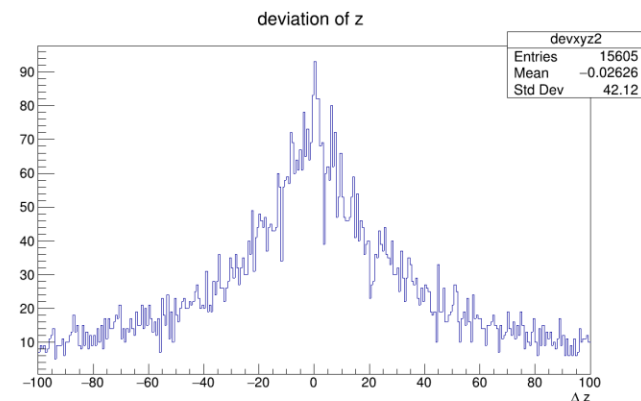
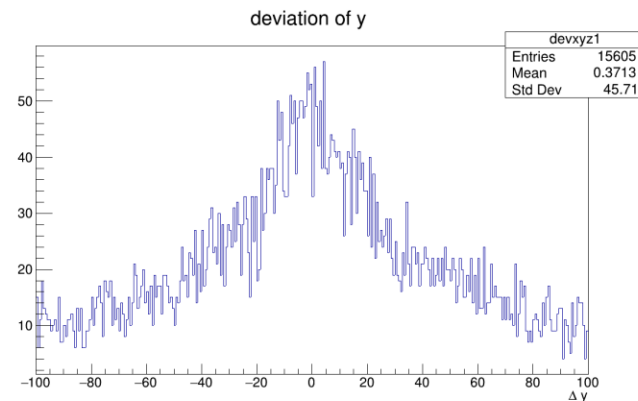
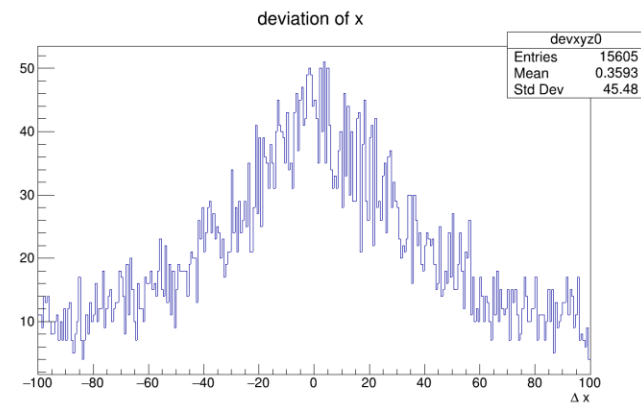
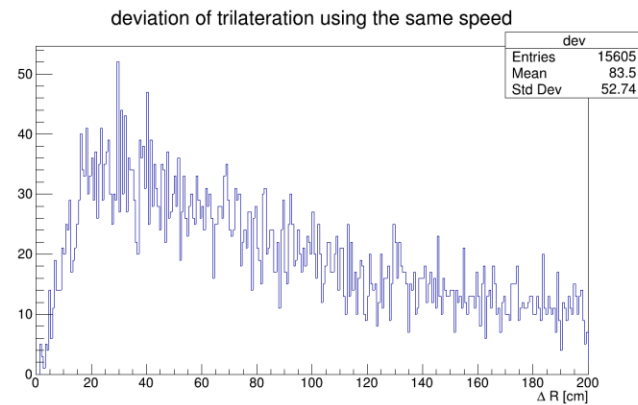
- T-B included  $3 < \text{hits}$
- 3 MeV threshold
- Get  $(x, y, z)$  by using the positions of the fastest 4 hits  
-> (Not only prompted pion but all particles)
- Test 3 cases :  
true flight lengths,  
the same speed,  
mean speed for each particle species

# Trilateration : true flight length

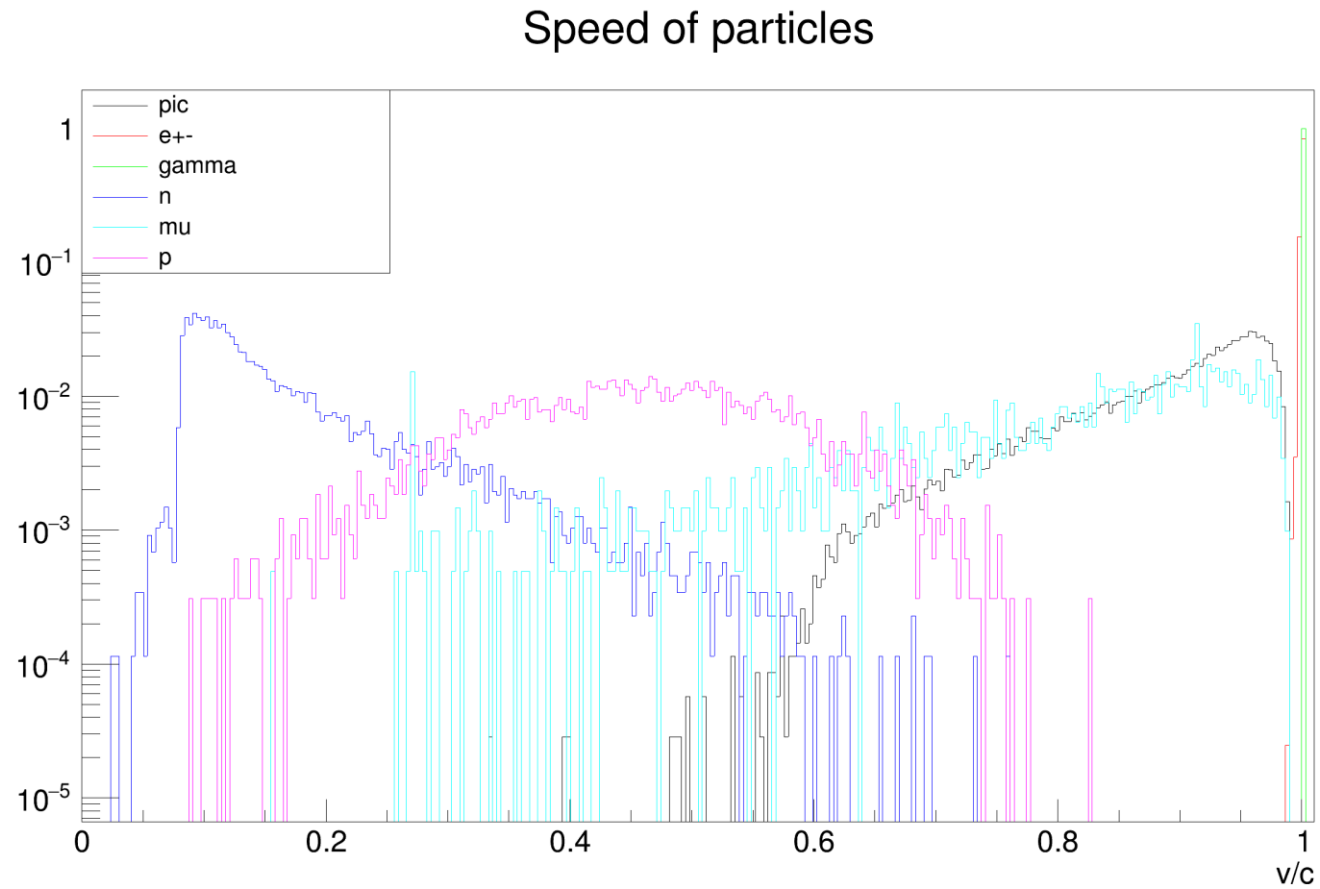


# Trilateration : the same speed

- Assume  $r_i = c(t_{i,hit} - t_{ann})$ , but we do not have information about  $t_{ann}$  in the real experiment.
- The result is also not good.



# Trilateration : the mean speed





# Trilateration : the mean speed

- Assume  $r_i = v_{i,mean}(t_{i,hit} - t_{ann})$
- The results highly depend on accuracy of  $r_i$ 's

